

WiZoom: Accurate Multipath Profiling using Commodity WiFi Devices with Limited Bandwidth

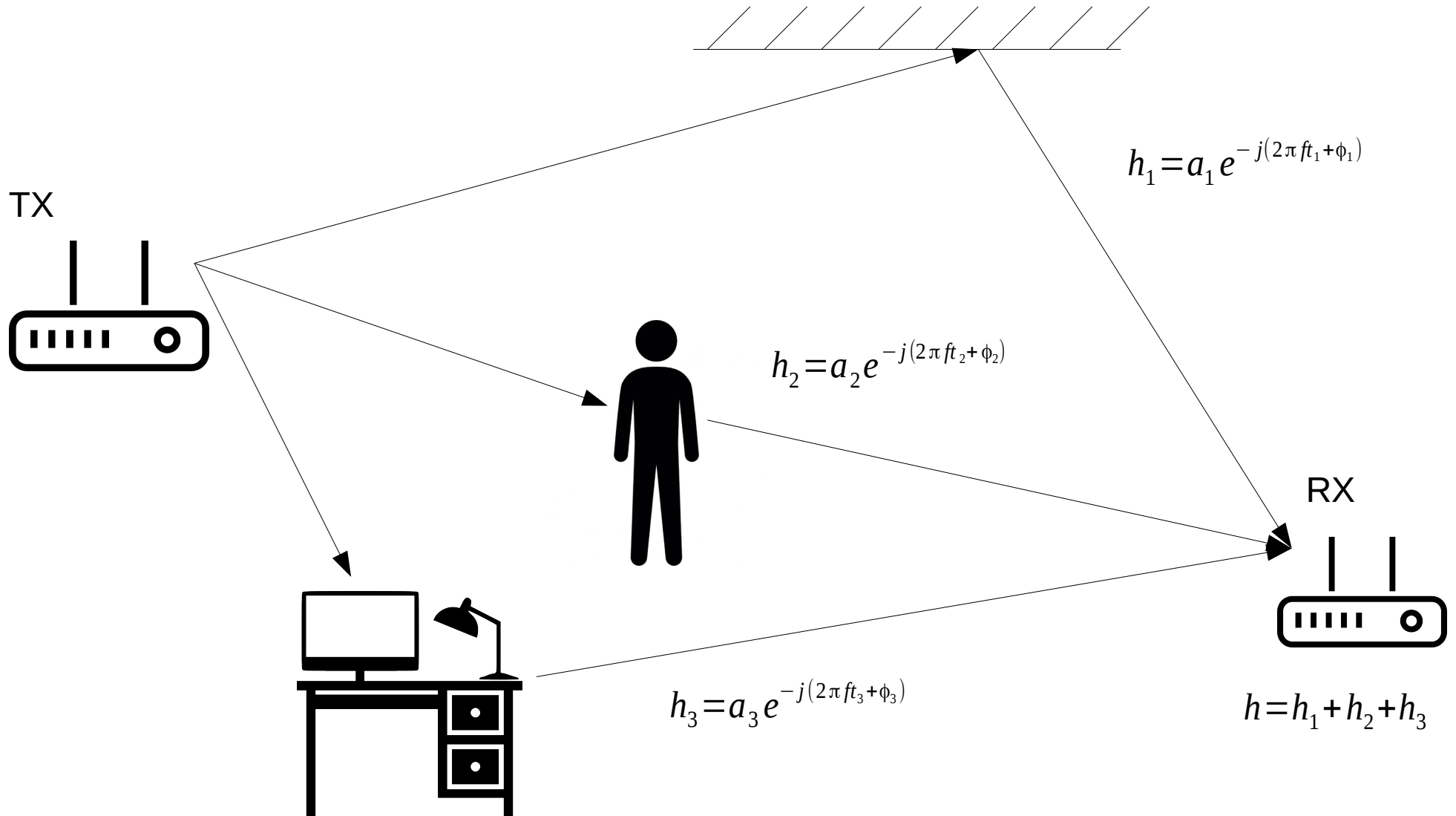
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Shanghai Jiao Tong University**



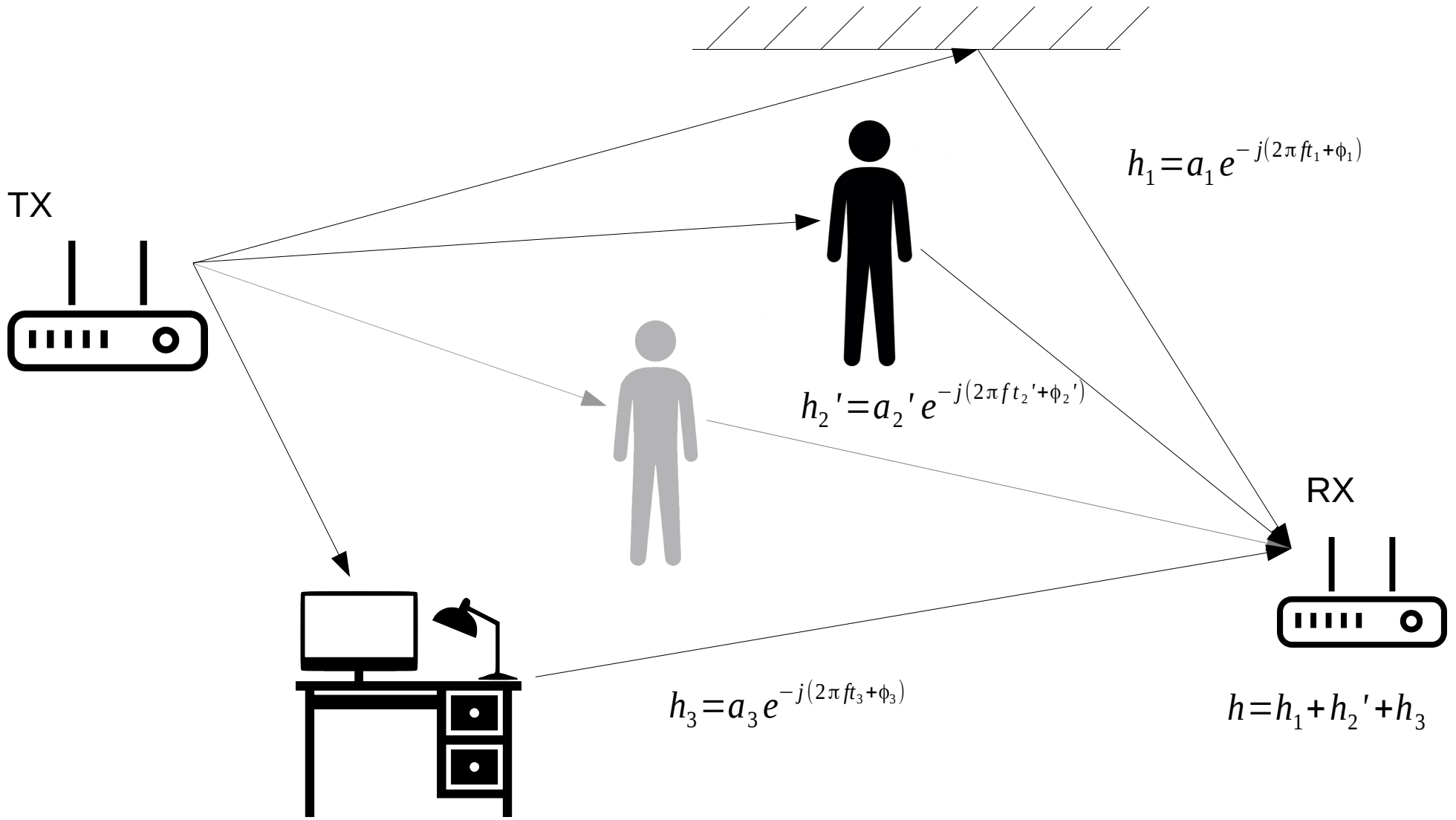
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Motivation

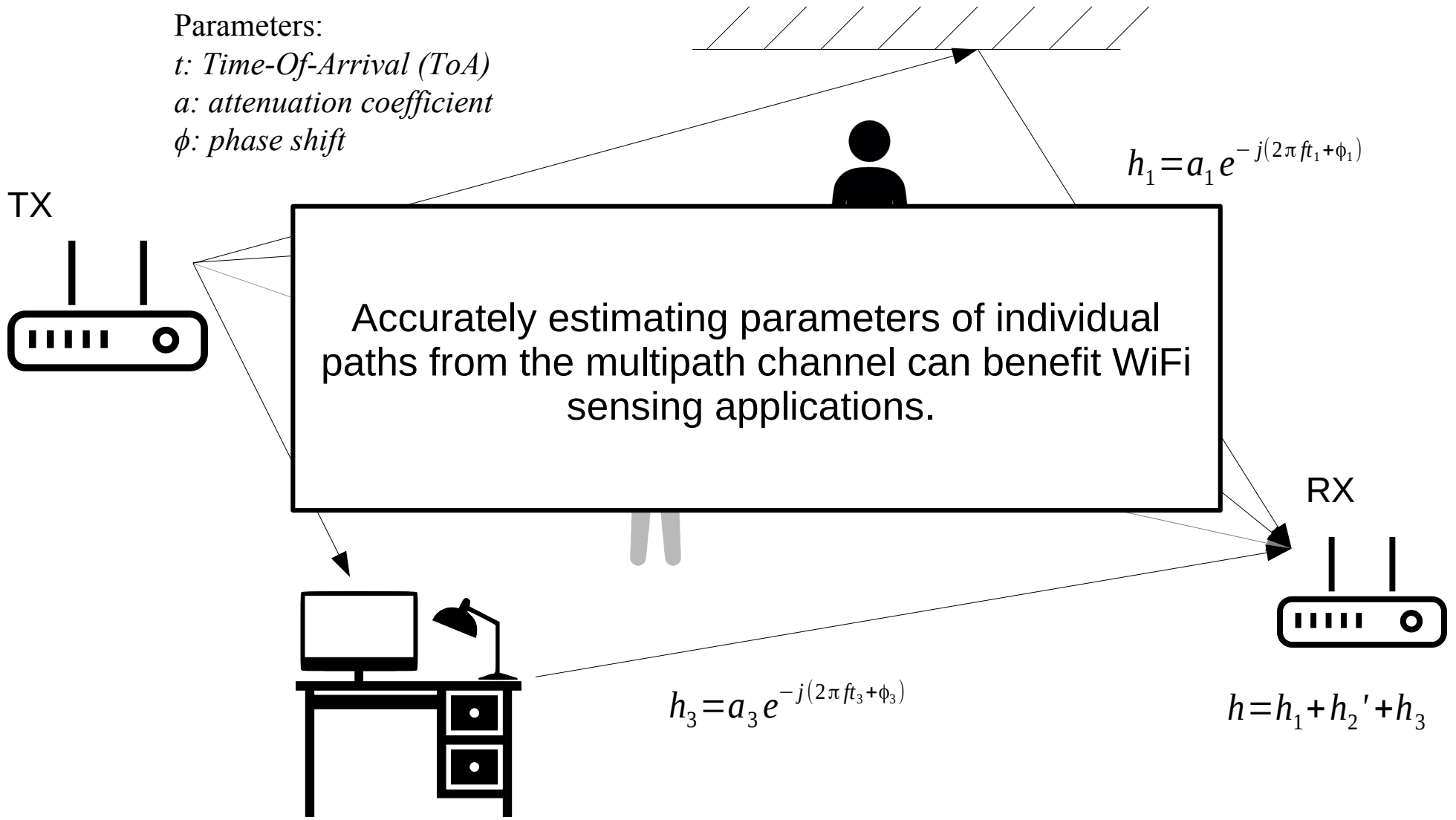


Motivation

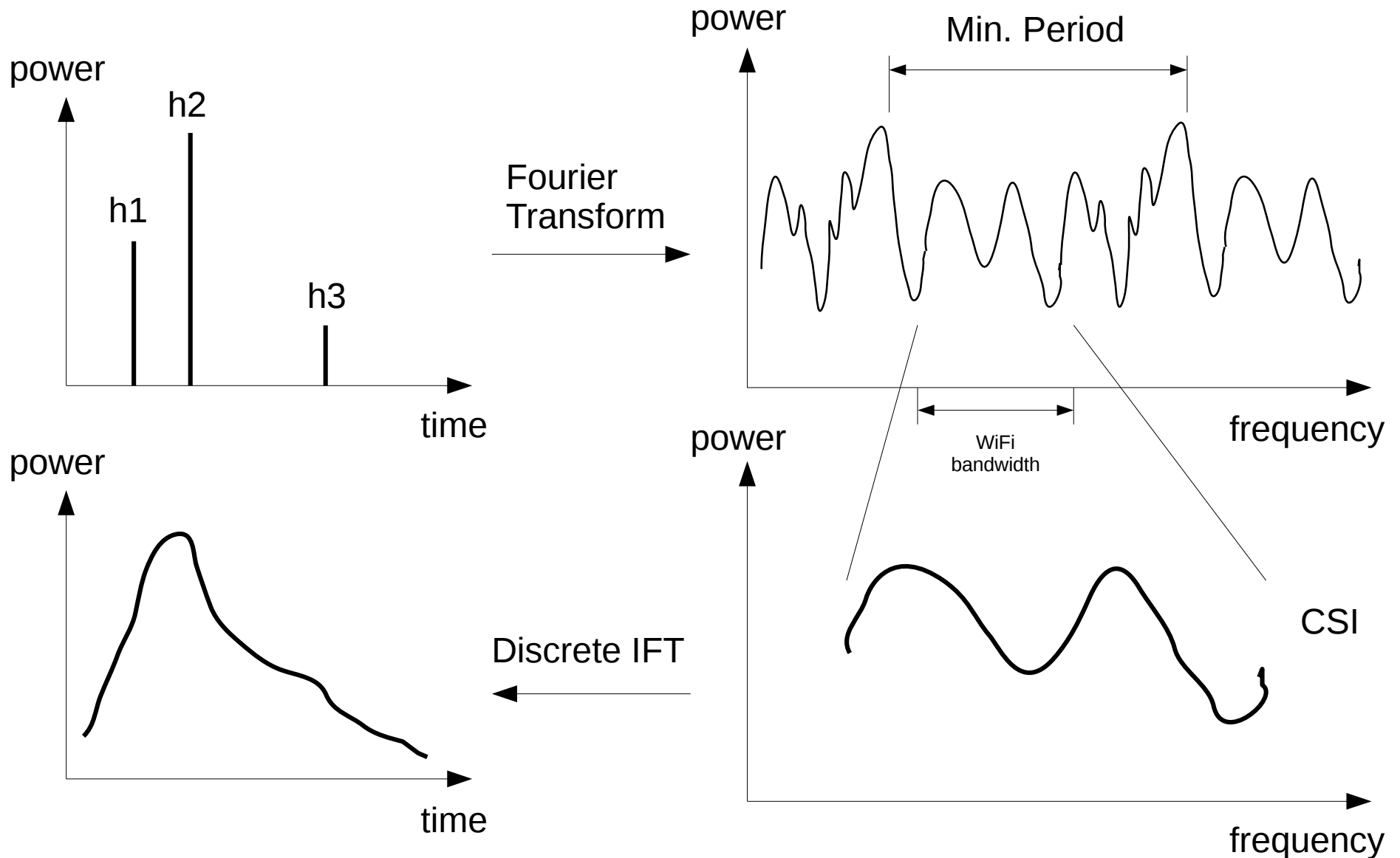


Motivation

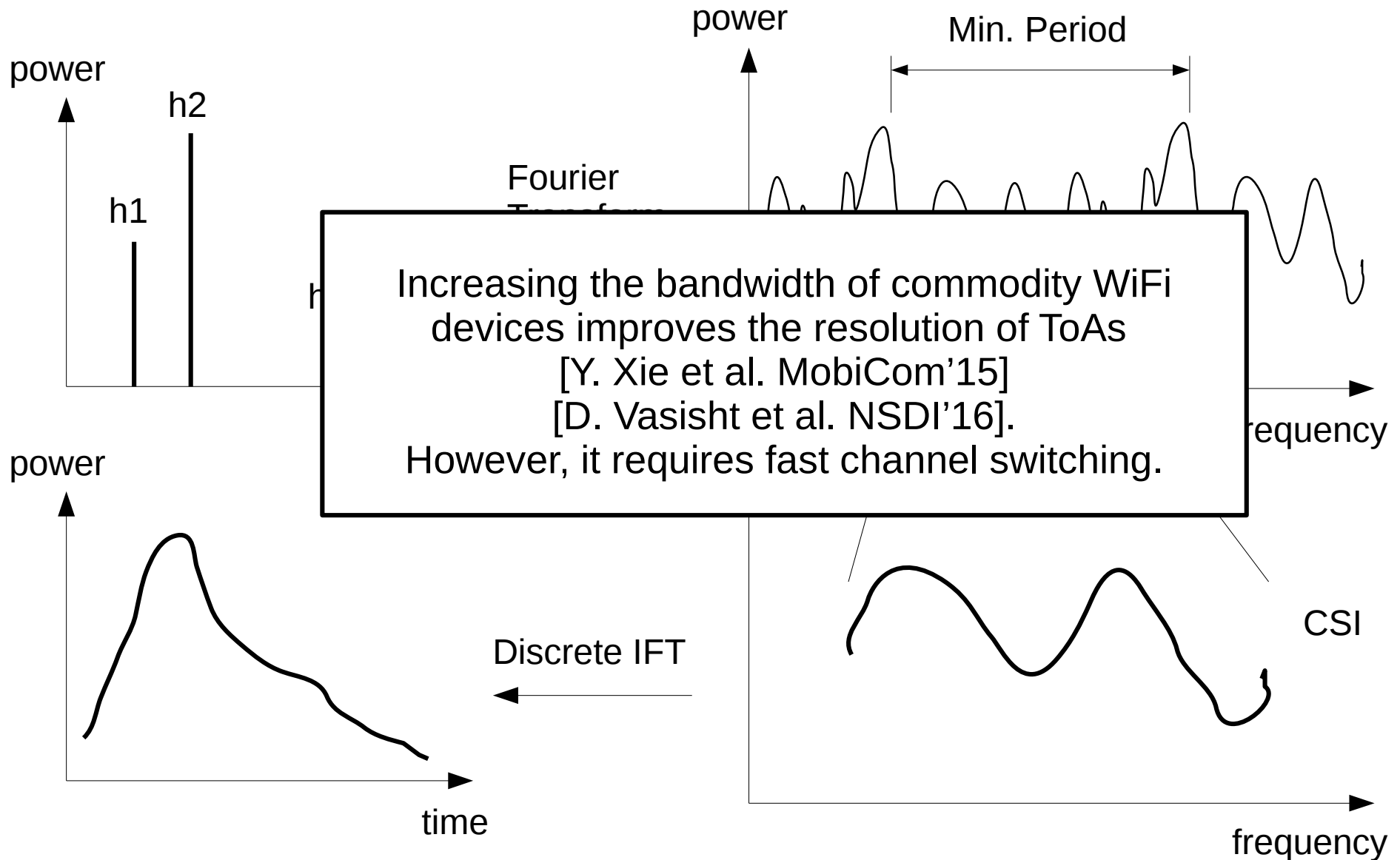
Parameters:
t: Time-Of-Arrival (ToA)
a: attenuation coefficient
φ: phase shift



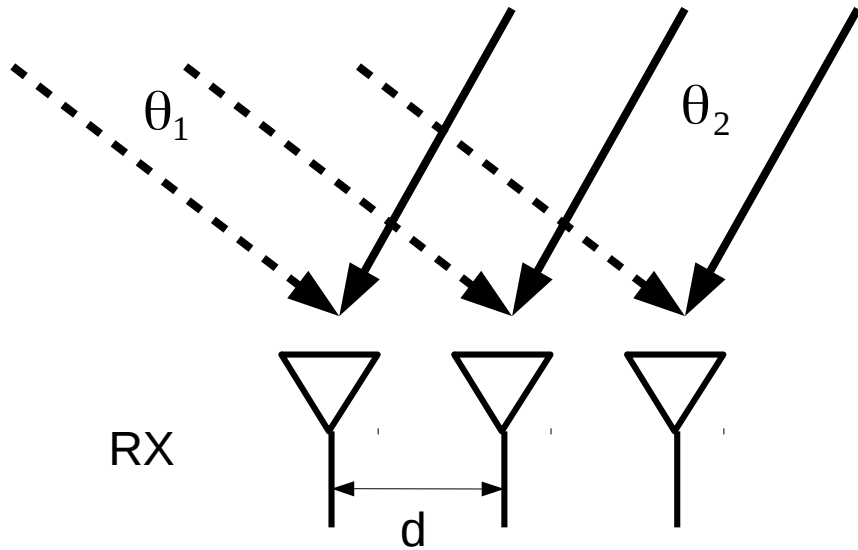
Challenge: Resolution



Challenge: Resolution



Remind: Resolution of AoA



Mode vectors:

$$a(\theta_1) = [1 \ e^{j2\pi d \cos \theta_1 / \lambda} \ e^{j2\pi 2d \cos \theta_1 / \lambda}]$$

$$a(\theta_2) = [1 \ e^{j2\pi d \cos \theta_2 / \lambda} \ e^{j2\pi 2d \cos \theta_2 / \lambda}]$$

MUSIC for AoA:

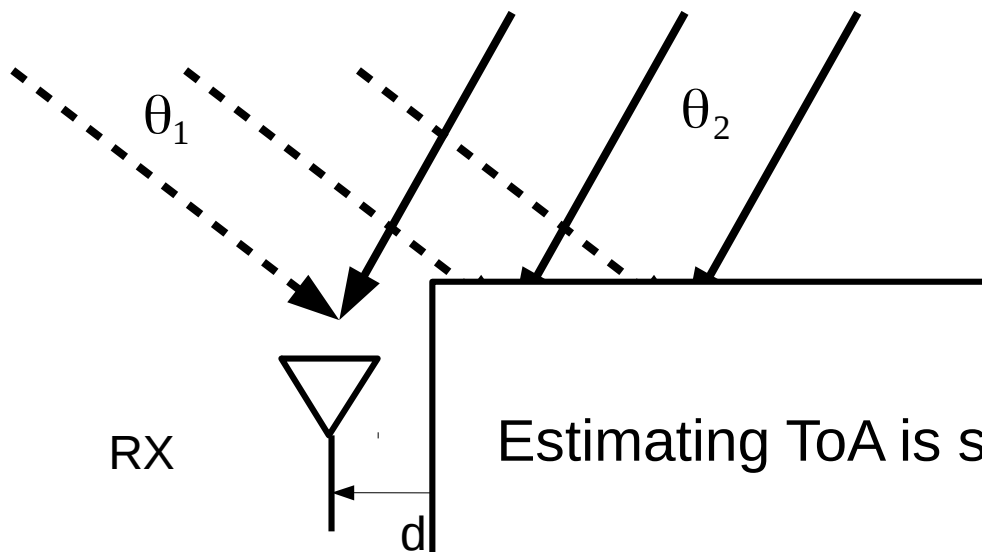
$$X = AF + W \quad A = [a(\theta_1)' \ a(\theta_2)']$$

Increasing the length of mode vectors can improve the resolution of AoA.

[M. Kataru et al. SIGCOMM'15] increases the length of mode vectors by incorporating different subcarriers:

$$A = \begin{bmatrix} 1 & 1 \\ e^{j2\pi \Delta_f t_1} & e^{j2\pi \Delta_f t_2} \\ e^{j2\pi 2\Delta_f t_1} & e^{j2\pi 2\Delta_f t_2} \\ \vdots & \vdots \\ e^{j2\pi d \cos \theta_1 / \lambda} & e^{j2\pi d \cos \theta_2 / \lambda} \\ e^{j2\pi (d \cos \theta_1 / \lambda + \Delta_f t_1)} & e^{j2\pi (d \cos \theta_2 / \lambda + \Delta_f t_2)} \\ e^{j2\pi (d \cos \theta_1 / \lambda + 2\Delta_f t_1)} & e^{j2\pi (d \cos \theta_2 / \lambda + 2\Delta_f t_2)} \\ \vdots & \vdots \\ e^{j2\pi 2d \cos \theta_1 / \lambda} & e^{j2\pi 2d \cos \theta_2 / \lambda} \\ e^{j2\pi (2d \cos \theta_1 / \lambda + \Delta_f t_1)} & e^{j2\pi (2d \cos \theta_2 / \lambda + \Delta_f t_2)} \\ e^{j2\pi (2d \cos \theta_1 / \lambda + 2\Delta_f t_1)} & e^{j2\pi (2d \cos \theta_2 / \lambda + 2\Delta_f t_2)} \\ \vdots & \vdots \end{bmatrix}$$

Remind: Resolution of AoA



Increasing the length of mode vectors can improve the resolution of AoA.

[M. Kataru et al. SIGCOMM'15] increases the length of mode vectors

subcarriers:

Estimating ToA is similar to estimating AoA!

Mode vectors:

$$a(\theta_1) = [1 \ e^{j2\pi d \cos \theta_1 / \lambda} \ e^{j4\pi d \cos \theta_1 / \lambda} \ \dots]$$

$$a(\theta_2) = [1 \ e^{j2\pi d \cos \theta_2 / \lambda} \ e^{j4\pi d \cos \theta_2 / \lambda} \ \dots]$$

MUSIC for AoA:

$$X = AF + W \quad A = [a(\theta_1)' \ a(\theta_2)']$$

$$A = \begin{bmatrix} 1 & e^{j2\pi(d \cos \theta_2 / \lambda + \Delta_f t_2)} \\ e^{j2\pi \Delta_f t_2} & e^{j2\pi(2 \Delta_f t_2)} \\ \vdots & \vdots \\ e^{j2\pi d \cos \theta_2 / \lambda} & e^{j2\pi(2 d \cos \theta_2 / \lambda)} \\ e^{j2\pi(d \cos \theta_1 / \lambda + \Delta_f t_1)} & e^{j2\pi(d \cos \theta_2 / \lambda + \Delta_f t_2)} \\ e^{j2\pi(d \cos \theta_1 / \lambda + 2 \Delta_f t_1)} & e^{j2\pi(d \cos \theta_2 / \lambda + 2 \Delta_f t_2)} \\ \vdots & \vdots \\ e^{j2\pi(2 d \cos \theta_1 / \lambda)} & e^{j2\pi(2 d \cos \theta_2 / \lambda)} \\ e^{j2\pi(2 d \cos \theta_1 / \lambda + \Delta_f t_1)} & e^{j2\pi(2 d \cos \theta_2 / \lambda + \Delta_f t_2)} \\ e^{j2\pi(2 d \cos \theta_1 / \lambda + 2 \Delta_f t_1)} & e^{j2\pi(2 d \cos \theta_2 / \lambda + 2 \Delta_f t_2)} \\ \vdots & \vdots \end{bmatrix}$$

The Analogy

- AoA estimation

- AoA introduces phase shift across different **antennas**.
- Apply MUSIC using **antennas** as sensors.
- Improve resolution:
Increase the number of sensors by incorporating **subcarriers**.

- ToA estimation

- ToA introduces phase shift across different **subcarriers**.
- Apply MUSIC using **subcarriers** as sensors.
- Improve resolution:
Increase the number of sensors by incorporating **antennas**.

The Analogy

- AoA estimation

- AoA introduces phase shift across different

antenn

- Apply M **antenn**

- Improv

Increase the number of sensors by incorporating **subcarriers**.

- ToA estimation

- ToA introduces phase shift across different

WiZoom uses this analogy and allocates all the resolution power to ToA estimation.

using sensors.

on:

Increase the number of sensors by incorporating **antennas**.

Estimate ToA

Signal model:

$$X = AF + W$$

$$A = \begin{bmatrix} 1 & 1 & \dots & 1 \\ e^{j2\pi\Delta_f t_1} & e^{j2\pi\Delta_f t_2} & \dots & e^{j2\pi\Delta_f t_k} \\ e^{j2\pi 2\Delta_f t_1} & e^{j2\pi 2\Delta_f t_2} & \dots & e^{j2\pi 2\Delta_f t_k} \\ \vdots & \vdots & \dots & \vdots \\ e^{j2\pi n\Delta_f t_1} & e^{j2\pi n\Delta_f t_2} & \dots & e^{j2\pi n\Delta_f t_k} \end{bmatrix} \begin{matrix} \updownarrow \\ z \end{matrix}$$

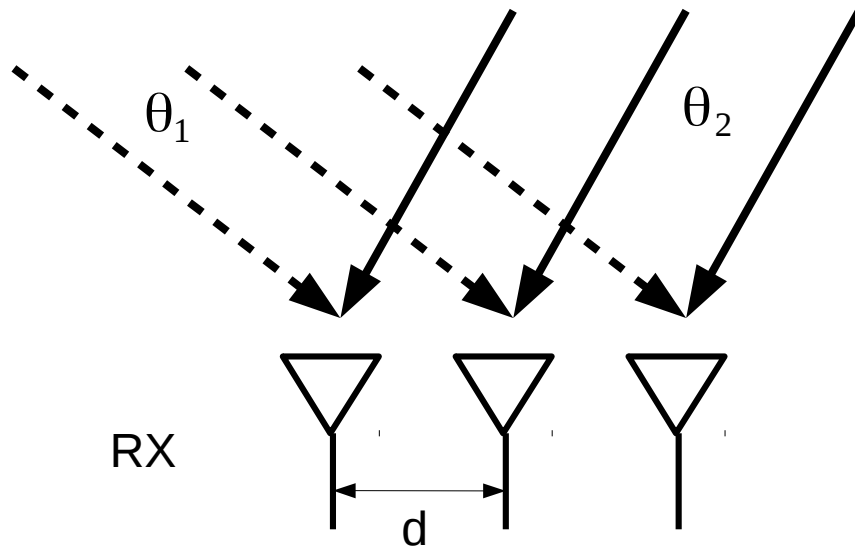
$$X = \begin{matrix} \leftarrow M \rightarrow \\ \begin{bmatrix} h(f_1) & h(f_2) & \dots & h(f_M) \\ h(f_{M+1}) & h(f_{M+2}) & \dots & h(f_{2M}) \\ h(f_{2M+1}) & h(f_{2M+2}) & \dots & h(f_{3M}) \\ \vdots & \vdots & \dots & \vdots \\ h(f_{NM}) & h(f_{(N-1)M+1}) & \dots & h(f_{NM}) \end{bmatrix} \begin{matrix} \updownarrow \\ z \end{matrix} \end{matrix}$$

#Subcarriers = $N * M$

MUSIC is applied to estimate (t_1, \dots, t_k)

Estimate ToA

Combine multiple antennas to improve resolution



$$h_{\text{antenna } 1} = h_1 + h_2$$

$$h_{\text{antenna } 2} = h_1 e^{j2\pi d \cos \theta_1 / \lambda} + h_2 e^{j2\pi d \cos \theta_2 / \lambda}$$

$$h_{\text{antenna } 2} = h_1 e^{j2\pi 2d \cos \theta_1 / \lambda} + h_2 e^{j2\pi 2d \cos \theta_2 / \lambda}$$

Channels of different antennas are **uncorrelated linear combinations** of multipath components.

The difference of ToAs between different antennas can be ignored.

Estimate ToA

Combine multiple antennas to improve resolution

$$\begin{array}{c}
 \xleftarrow{\hspace{10em} M * \# \text{antennas} \hspace{10em}} \\
 X = \begin{bmatrix}
 h_1(f_1) & .. & h_1(f_M) & h_2(f_1) & .. & h_2(f_M) & .. \\
 h_1(f_{M+1}) & .. & h_1(f_{2M}) & h_2(f_{M+1}) & .. & h_2(f_{2M}) & .. \\
 h_1(f_{2M+1}) & .. & h_1(f_{3M}) & h_2(f_{2M+1}) & .. & h_2(f_{3M}) & .. \\
 \vdots & .. & \vdots & \vdots & .. & \vdots & .. \\
 h_1(f_{NM}) & .. & h_1(f_{NM}) & h_2(f_{NM}) & .. & h_2(f_{NM}) & ..
 \end{bmatrix}
 \begin{array}{c}
 \xrightarrow{\hspace{1em} z \hspace{1em}} \\
 \downarrow
 \end{array}
 \end{array}$$

(Total # of Elements) = (# of Subcarriers) * (# of Antennas)

This means we can further increase N to improve resolution.

Estimate other path-related parameters

Channel model:

$$h(f) = \sum_{i=1}^N a_i e^{-j(2\pi f t_i + \phi_i)}$$

of equations = # of subcarriers

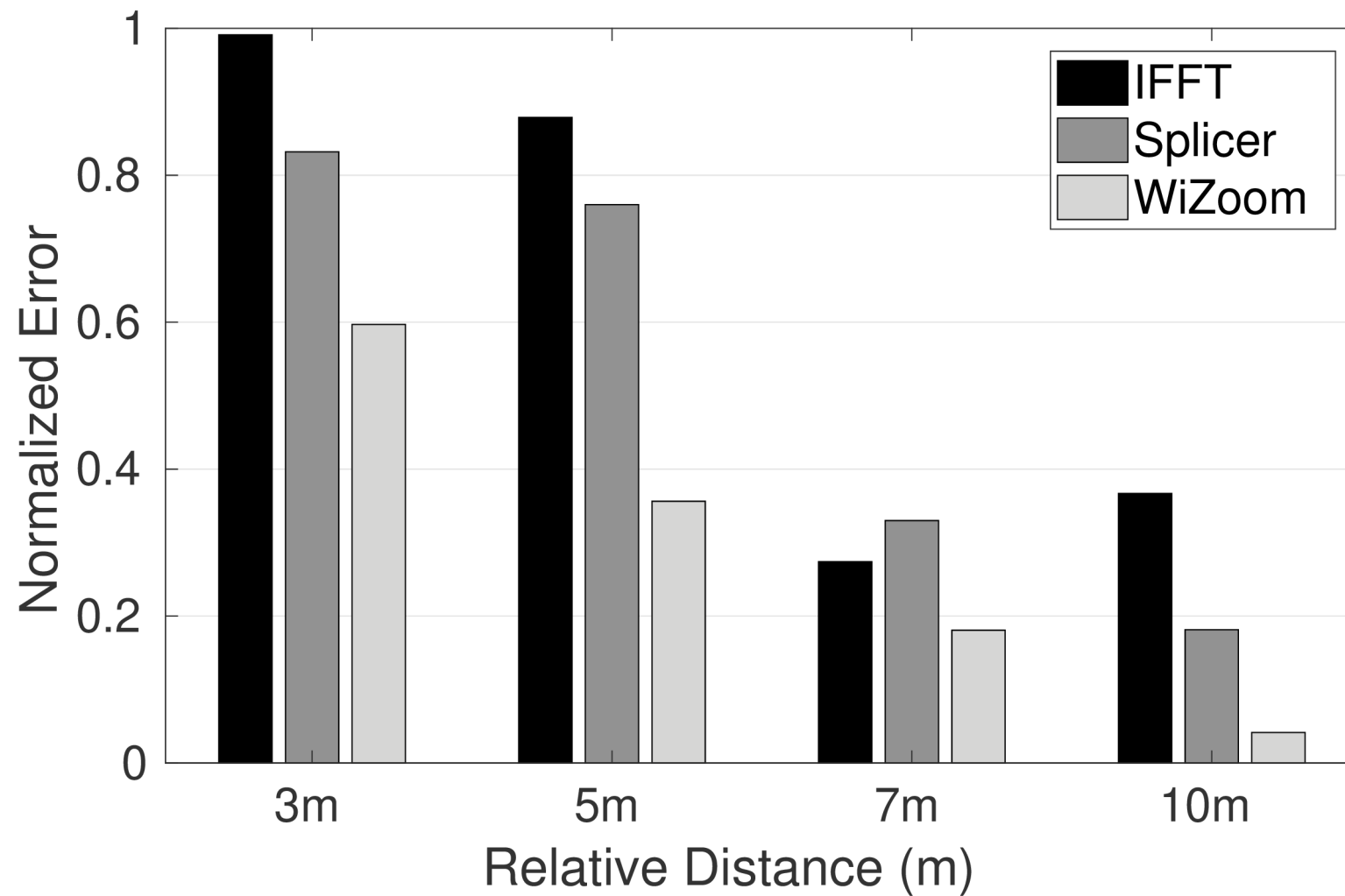
of unknowns = # of multipath components

Solve this linear system using Least Square.

Evaluation

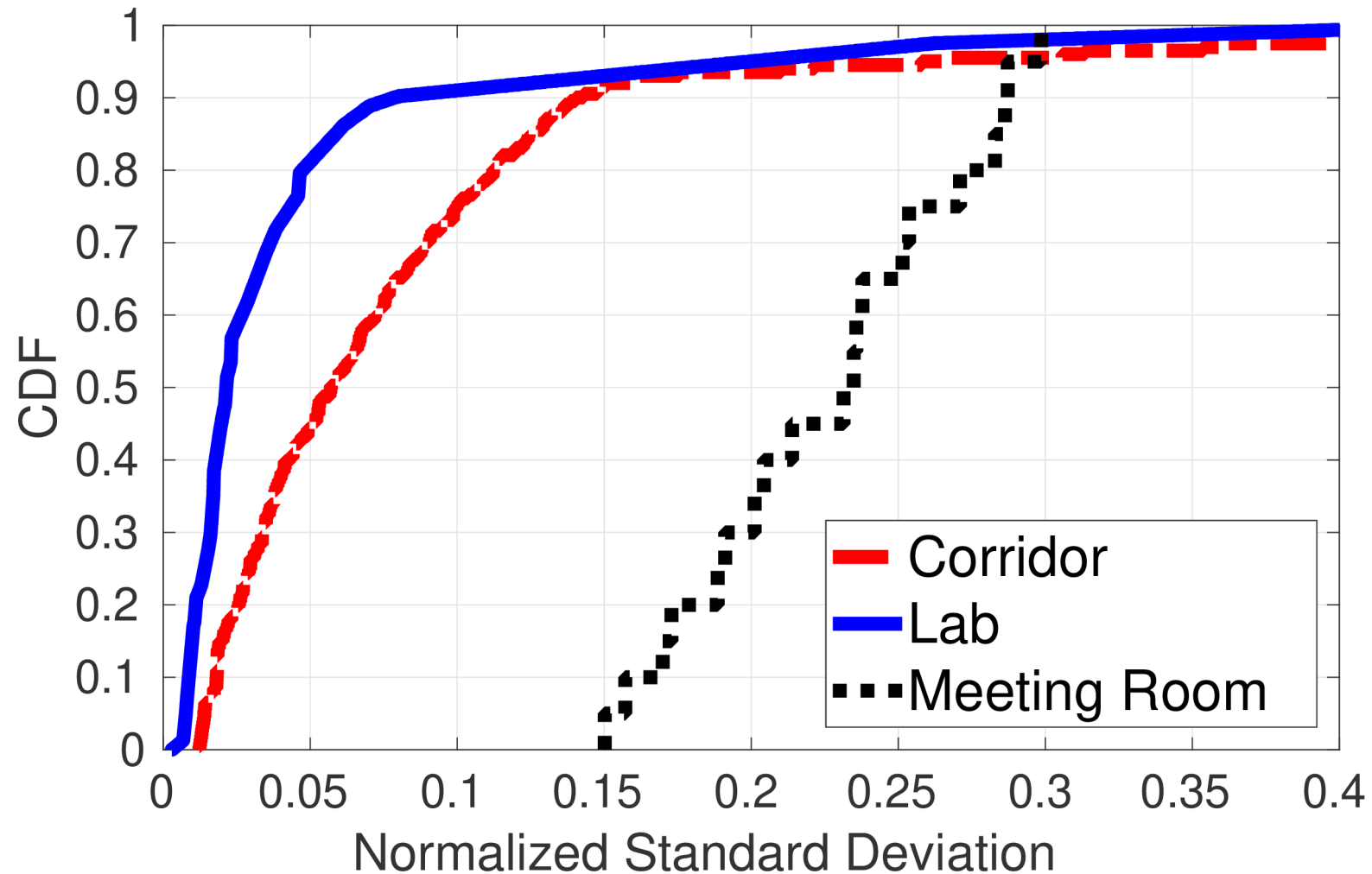
- Ideal case benchmark
 - Use RF cables, attenuators and splitters to emulate multipath channels of WiFi signal.
 - Different length of RF cables emulate different signal propagation paths, which induces different ToAs
- Real environment evaluation
 - Lab: 13*13m, 200 locations, distance of [1,12]m
 - Corridor: 3*50m, 200 locations, distance of [1,50]m
 - Meeting room: 3*5m, 20 locations, distance of 3m

Ideal case



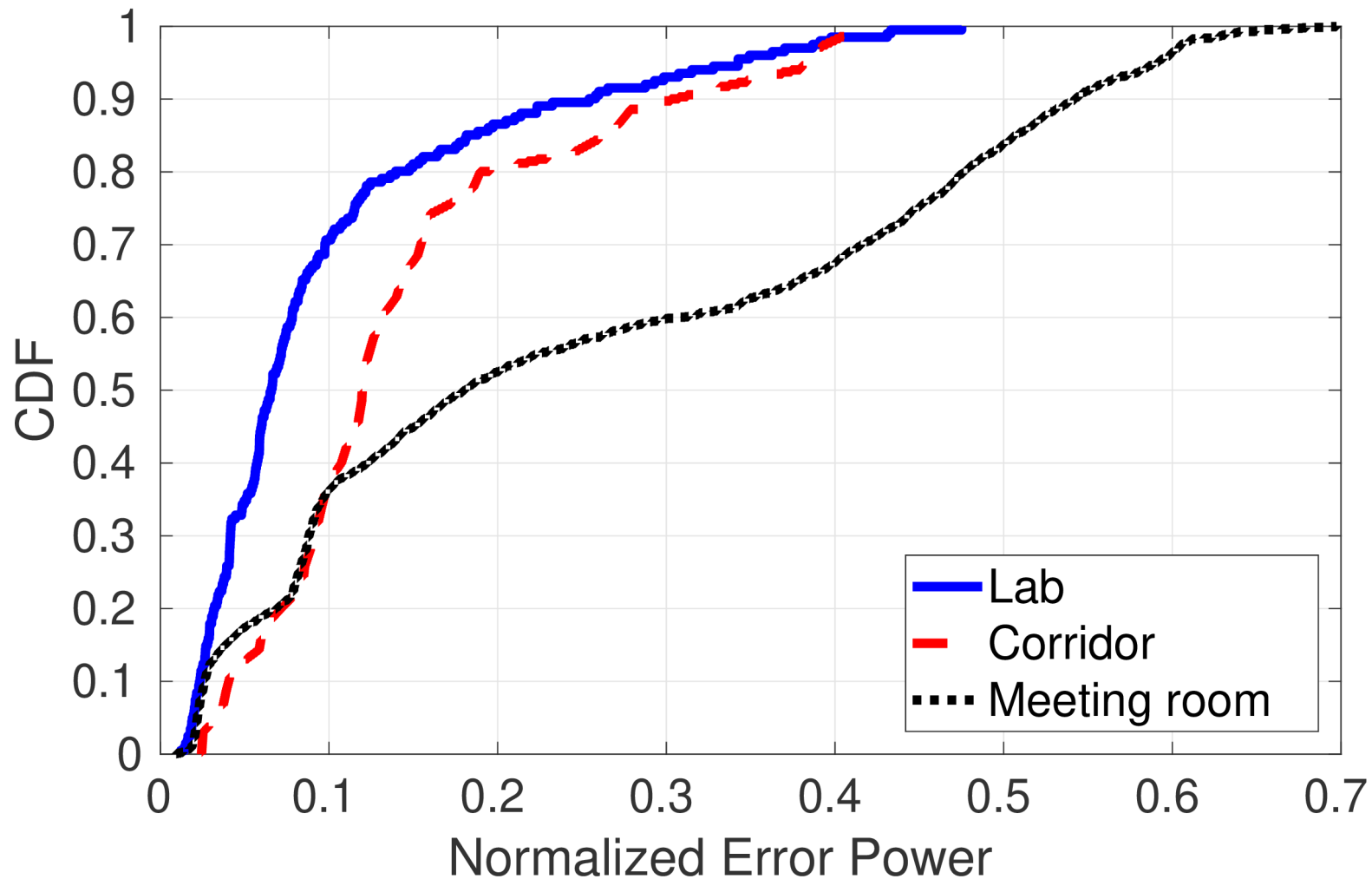
Real Environment

- Stability of direct path attenuation



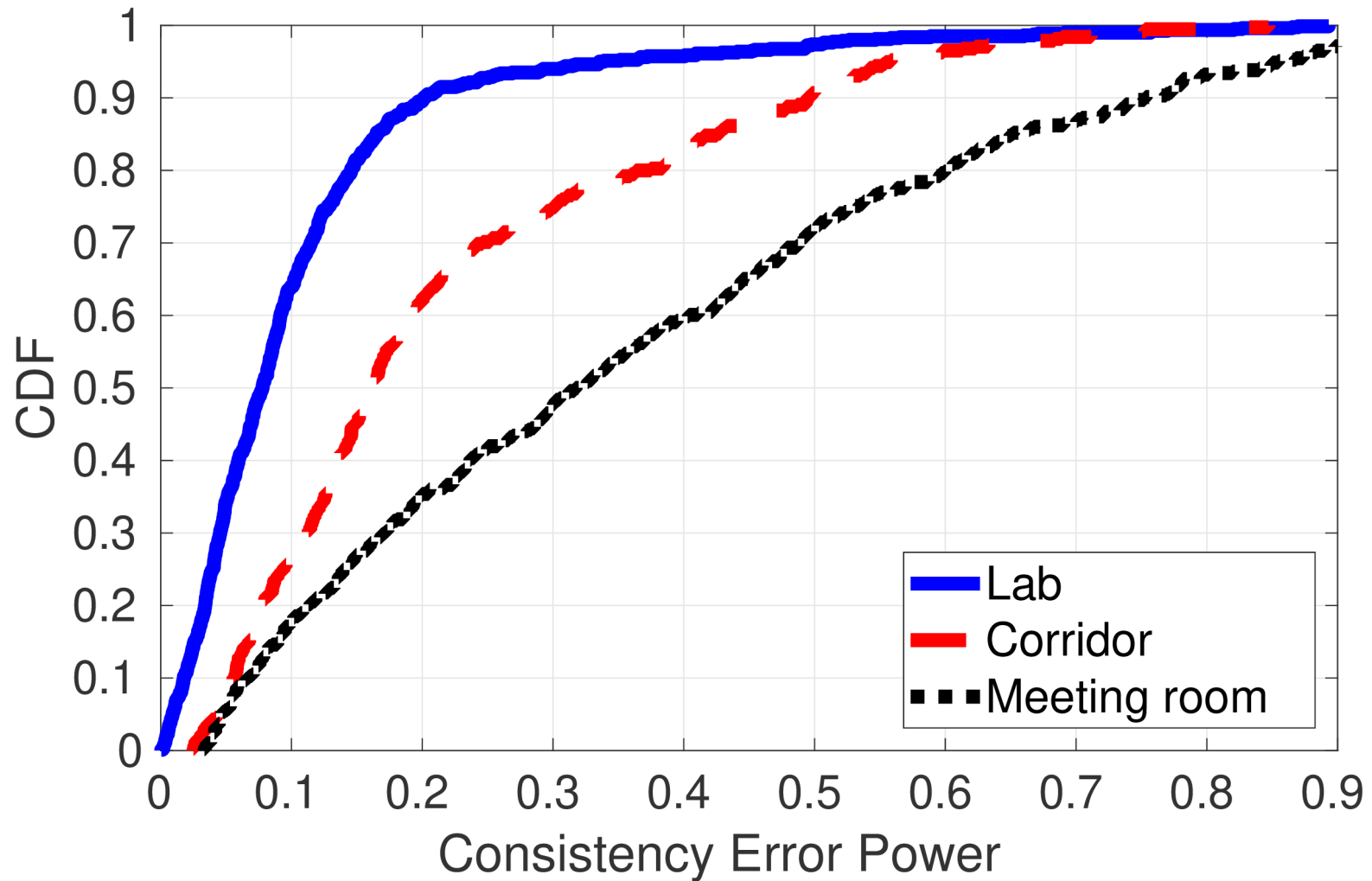
Real Environment

- CSI fitting performance



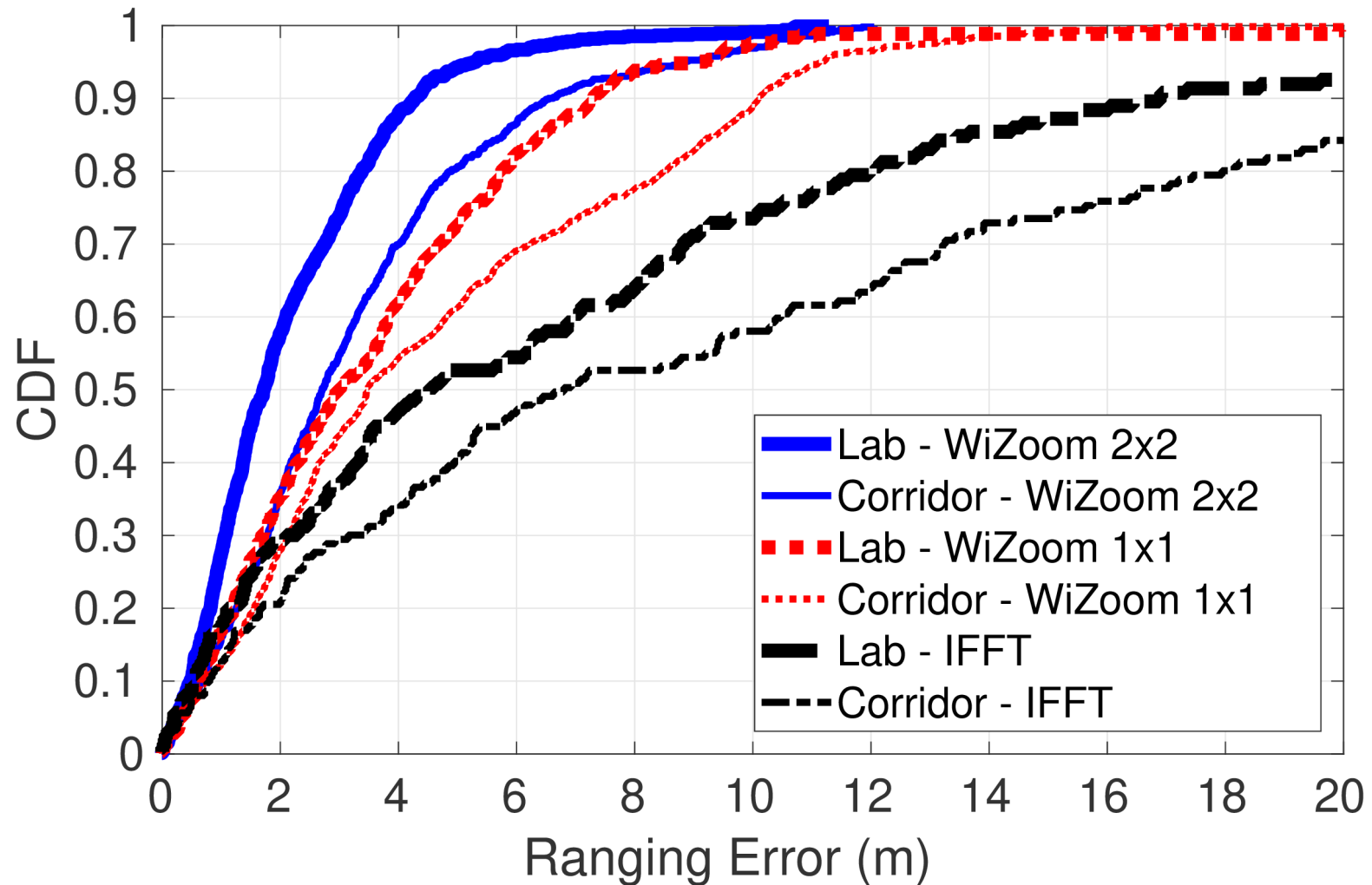
Real Environment

- Consistency across different antennas



Real Environment

- Ranging error



Conclusion

- We tackle the problem of multipath profiling using commodity WiFi devices with limited bandwidth.
- We design a scheme called WiZoom, which uses a MUSIC-based algorithm and combines multiple antennas to estimate ToAs with high resolution.
- WiZoom also estimates other path-related parameters to form the complete multipath profile.
- We evaluate the performance of WiZoom and the results show that WiZoom outperforms existed methods.

Thank you all!

Further question? Hua Xue: howardsid@sjtu.edu.cn



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